Effect of Ce cations on the crystallite size and pore structure genesis in nanostructured rutile after calcination

N. V. Shikina¹, E. V. Bessudnova¹, V. A. Ushakov¹, A. P. Nikitin², M. S. Mel'gunov¹, A. V. Ishchenko¹, Z. R. Ismagilov^{1,2}

¹Boreskov Institute of Catalysis SB RAS, 5 Lavrentiev Ave., 630090, Novosibirsk, Russia ²Institute of Coal Chemistry and Materials Science, Federal Research Center of Coal and Coal Chemistry SB RAS, 18 Sovetskiy pr., 650000, Kemerovo, Russia

shikina@catalysis.ru

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A method for the low-temperature synthesis of titania with the 3D rutile nanostructure was developed, and the effect of introduced cerium ions on the thermal stability of the material was studied. According to XRD, TEM, Raman spectroscopy and BET data, the introduction of 3 - 10 wt.% Ce into the rutile matrix decreases the growth of nanorutile crystallites under the action of high temperatures ranging from 300 - 1000 °C and provides the formation of a more porous structure in comparison with unmodified samples. Cerium cations are stabilized in the region of interblock boundaries or in the structural defects of rutile TiO₂ and are released as the bulk CeO₂ phase only at 1000 °C, which does not exert a stabilizing effect at this temperature.

Keywords: titanium dioxide, nanostructured rutile, hierarchical architecture, porous structure, thermal treatment.

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1. Introduction

In recent years, the study of TiO_2 hierarchical nanostructures has been a hot topic of research in the field of effective photocatalytic materials due to their high specific surface area, beneficial light absorption, and appropriate refractive index, along with other excellent physical and chemical properties [1–3]. The potent photocatalytic properties of TiO_2 hierarchical nanostructures with rutile modification have been established in degradation of methyl orange, methylene blue and brilliant red X-3B [4–7]. Rutile TiO_2 has a high refractive index, which determines its application not only in photocatalysis but also in optical filters, protected printing and production of cosmetics and dyes [8].

Bulk rutile is the most stable phase among polymorphous modifications of titania (anatase, brookite and rutile). The formation of rutile from anatase or amorphous TiO_2 species occurs after reaching a critical size of the particles and temperatures above 465 °C. At the polymorphous transition temperatures the particles agglomerate and the specific surface area decreases below 7 m²/g [9]. The emphasis is now focused on the development of synthetic strategies for nanostructured titania that would permit its controllable three-dimensional formation. TiO₂ synthesis under conditions leading to the formation of 3D structures with hierarchical packing of nanostructured particles makes it possible to obtain a material with the stable rutile phase and high specific surface area [10].

The properties of a composite hierarchical system are determined mostly by the properties of agglomerated particles, their packing and morphology, i.e. the texture of the material. Hierarchical rutile TiO_2 microspheres assembled by nanowire bundles were synthesized upon hydrothermal conditions and then treated by thermally annealed in [4]. T. Yan and co-authors relate structural defects and high functional properties of rutile to the "microcavity" structure which existed between the roughly parallel nanowires of TiO_2 microspheres. Upon annealing at 300 and 500 °C the microspherical shape was maintained, whereas the interface of the nanowire bundles became blurred and the related microstructural feature greatly changed. At 700 °C, nanowires were converted into larger nanorods. The authors attribute such integration between quasi-parallel nanowires to a possible growth of crystals in the perpendicular direction. It is clear that the annealing treatment seriously destroyed the microcavity structure.

Our earlier studies [11–13] demonstrated the possibility of obtaining rutile with a hierarchical 3D nanostructure composed of fan-shaped nanofibers (specific surface area > 140 m²/g) at atmospheric pressure and a temperature below 100 °C. This revealed the control the main synthesis parameters (e.g. temperature, concentration of Ti⁴⁺ and Cl⁻ ions) had on the formation of the rutile phase. However, the produced material has a low crystallinity and a high defect content and interblock boundaries, which determine the low stability of its textural properties after thermal treatment [14]. Changes in the morphology of the material were observed at the 300 – 400 °C, lower than temperatures previously reported in [4]. The enhancement of thermal stability of the material is a topical task

because textural characteristics of nanostructured rutile are of key importance for its application as a support of catalysts or photocatalysts.

In [15–17], titania was modified with different metal cations, shifting the anatase \rightarrow rutile polymorphous transformations to higher temperatures, which is accomplished by inhibiting the growth of crystallites stabilized by CeO₂ [15], SiO₂ [16] or Y₂O₃ [17] interlayers. Such modification results in the formation of nanocrystalline anatase structure comprising incoherently intergrown particles; this significantly hinders the growth of anatase crystallites to the critical values at which anatase converts to rutile. In [18, 19] it was shown that modification with La and Ce ions [18] or La and Mg ions [19] stabilizes the alumina pore structure and specific surface area. The authors revealed a relation between the effect exerted by metal cations on polymorphous transformations in alumina and its structural-mechanical properties.

In the present work, we explored the possibility of decreasing rutile crystallite growth and preventing the deterioration of its pore structure parameters during thermal treatment upon modification of the initial low-temperature rutile samples with cerium cations. Since rutile is a stable phase of titania, it is evident that polymorphous transformations will not occur; however, the formation of the stabilizing ceria interlayers in nanostructured rutile may hinder the growth of nanofiber crystallites in the perpendicular direction.

2. Experimental

The method employed for the synthesis of nanostructured rutile is described in detail in [13]. Briefly, titania (rutile) was synthesized by the sol-gel method via the hydrolysis of titanium tetrachloride in water under the following conditions: molar ratios $[Cl^{1-}]/[Ti^{4+}] = 4$ and $[H_2O]/[Ti^{4+}] = 39$, and the hydrolysis temperature of 90 °C. To improve thermal stability, an aqueous solution Ce(NO₃)₃·6H₂O was deposited on the dried rutile powder by incipient wetness impregnation to obtain 3, 5, 7 and 10 wt.% CeO₂ content in the final samples. After that, the samples with different CeO₂ content were calcined at 300, 500, 700 and 1000 °C. A series of rutile samples modified with ceria was examined by XRD, BET, Raman spectroscopy and TEM. A rutile sample without CeO₂ served as the reference sample.

The chemical compositions of the synthesized samples were estimated by inductively coupled plasma atomic emission spectroscopy on an Optima 4300 DV instrument and by X-ray fluorescence analysis on an ARL-Advant'x analyzer with an Rh-anode X-ray tube. XRD studies were performed using an HZG-4C (Freiberger Präzisionsmechanik) X-ray diffractometer with a CoK α monochromatic source ($\lambda = 1.79021$ Å) in a continuous mode over the 2θ angular range from 20 to 85° . Crystallite sizes were estimated by the Scherrer formula. The measurement error is in the range of: $30 - 50 \pm 2$; $50 - 80 \pm 5$; $80 - 120 \pm 10$; $120 - 180 \pm 25$; $180 - 250 \pm 40$; $250 - 300 \pm 80$ Å. Raman spectroscopy studies were carried out on a Renishaw Invia Basis spectrometer at 3600 - 100 cm^{-1} . Textural properties (specific surface area and pore volume) were analyzed by low-temperature nitrogen adsorption (ASAP-2400, Micromeritics) and mercury porosimetry (AutoPore IV 9500 V1.09, Micromeritics). The measurement error of textural parameters is 5 %. Transmission electron microscopy (TEM) and high resolution transmission electron microscopy (HR-TEM) images were obtained using a JEM-2010 (JEOL, Japan) microscope.

3. Results and discussion

Particles of the material obtained by TiCl₄ hydrolysis belong to the rutile phase and have an intricate packing system; their characteristics correspond to those of 3D hierarchical structures. At the first structural level, the primary particles coherently inter-grow to form nanofibers. The oriented addition of the primary particles includes a spontaneous self-organization of adjacent particles due to which they become involved in the joint crystallographic orientation with subsequent agglomeration of the particles at the plane interface [20]. Binding of the particles decreases the total energy of their aggregates due to the surface energy of uncompensated bonds of primary particles, thus leading to the coherent intergrowth of particles, which is more favorable in terms of energy. Nanofibers forming the first structural level are joined into the fan-shaped aggregates that constitute the second structural level. At the third level the aggregates merge into large 3D particles [13].

3.1. XRD

X-ray diffraction (XRD) studies of the samples showed that the crystallite size of rutile is 55 - 70 Å along the (110) direction and 140 - 200 Å along (002) [11]. A clear dependence of crystallite sizes on the synthesis temperature was not observed. However, substantial changes in the crystallite size were revealed after calcination of the samples at 300, 500, 700 and 1000 °C (Table 1). Upon calcination at 300 - 500 °C the crystallite size of rutile increased 2 - 3-fold, and calcination at 700 and 1000 °C resulted in the formation of large crystallites with the size greater than 1000 Å along all crystallographic directions. Thus, calcination at temperatures above 700 °C does not produce noticeable changes in the XRD pattern of the samples.

The rutile samples modified with cerium cations also showed an increase in the crystallite size upon calcination (Table 1). However, the crystallite size of the samples with Ce is much smaller in all crystallographic directions as compared to the rutile samples without cerium addition at a temperature up to 700 °C. On diffraction patterns of the rutile samples modified with 3 - 10 % CeO₂, the bulk ceria phase manifests itself only after calcination at 1000 °C (Fig. 1); at this temperature ceria does not exert a stabilizing effect. The crystallite size of the 1000 °C samples strongly exceeds 1000 Å both in the modified rutile series and in the samples without additives. Peaks corresponding only to the rutile phase are observed on diffraction patterns of the samples calcined at 300 – 700 °C. Peaks corresponding to the interaction phases in the Ce–Ti–O system were also not detected, and the crystal lattice parameters of rutile correspond to those of pure rutile. Supposedly, ceria is in a highly dispersed state and is located mostly on the surface of rutile crystallites, thus preventing their intergrowth upon calcination.

T_{calc} , °C	CeO ₂ , %	Crystallite sizes (E) along crystallographic directions				
	-	110	101	111	211	002
		32.00 °	42.19 °	48.30	64.09°	74.45°
After synthesis 90	0	60	130	120	70	165
300	0	125	200	190	140	230
	3	95	170	170	100	230
	5	70	170	170	95	230
	7	70	170	170	95	230
	10	70	170	170	95	230
500	0	190	250	240	200	250
	3	140	200	200	130	250
	5	110	200	200	150	250
	7	110	200	200	150	250
	10	110	200	200	150	250
700	0	≫1000	≫1000	≫1000	≫1000	≫1000
	3	220	400	300	160	190
	5	180	270	300	160	190
	7	170	210	270	150	200
	10	170	180	250	150	200
1000	0	≫1000	≫1000	≫1000	≫1000	≫1000
	3	≫1000	≫1000	≫1000	≫1000	≫1000
	5	≫1000	≫1000	≫1000	≫1000	≫1000
	7	≫1000	≫1000	≫1000	≫1000	≫1000
	10	≫1000	≫1000	≫1000	≫1000	≫1000

TABLE 1. Crystallite sizes of the calcined samples of nanostructured rutile with different ceria content

3.2. Raman spectroscopy

Rutile has only three active modes in the Raman spectra: $145A_{1g}$, $447E_g$, and $612B_{1g}$ [21]. Along with the indicated modes, a peak at ca. 240 cm⁻¹, which can be assigned to the composite vibration, appears in the spectrum. Ceria has a cubic crystal structure of the fluorite type and manifests only one resolved combination mode, $465F_{2g}$ [22]. The Raman data obtained for the samples of pure rutile and rutile with the addition of 5 % CeO₂ are listed in Table 2.

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FIG. 1. The diffraction pattern of the rutile samples modified with 5 % CeO₂ after their calcination at 300, 500, 700 and 1000 °C (peaks corresponding to the CeO₂ phase are marked by asterisks)

$T_{calcination}, \ T_{synthesis}, \ ^{\circ}\mathrm{C}$	Position of main peaks / Half-width, cm ⁻¹				Additional peaks, cm ⁻¹	
Rutile + 5 % CeO ₂						
100	141 / 5	234 / 77	444 / 45	608 / 45	822, 1601	
300	142 / 4	248 / 68	424 / 71	606 / 76	169 / 12, 1597	
500	141 / 4	242 / 92	433 / 55	607 / 63	167 / 7, 1599	
700	141 / 5	234 / 87	442 / 43	608 / 50	821, 1603	
1000	142 / 5	234 / 87	444 / 44	609 / 45	821, 1606	
Rutile						
90	_	239 / 63	437 / 49	605 / 55	1601	
300	145 / 12	234 / 67	440 / 56	608 / 54	821, 1601	
500	142 / 8	233 / 81	442 / 43	609 / 48	821, 1602	
700	142 / 6	231 / 89	444 / 39	609 / 43	819, 1603	
1000	142 / 5	231 / 87	444 / 39	608 / 44	824, 1604	

TABLE 2. Main and additional peaks of rutile in the Raman spectra

For all the samples, the B_{1g} peak did not change its position. In the case of rutile samples synthesized without CeO₂, the half-width of the B_{1g} peak decreased with raising the temperature from 55 to 43 cm⁻¹, which testifies to the growth of crystallites. For the modified samples, at a calcination temperature of 300 °C the half-width of this peak increased from 45 to 76 cm⁻¹, which indicates a decrease in the size of initial nanoparticles or a structural disordering with an increase in the bond length between atoms in the crystal lattice at the retained translational symmetry. This may occur due to intercalation of cerium cations between crystallites in the region of interblock boundaries where the rutile structure is strongly disordered, which makes the structural defects even more pronounced. As the temperature is raised to 1000 °C, the half-width of the B_{1g} peak decreases, similar to the case without CeO₂. The main active vibration of CeO₂ does not appear in the Raman spectra up to 1000 °C.

The most pronounced changes in the E_g peak of the modified Ce samples are observed upon calcination at 300 °C: the position of the peak shifts to the red region from 444 to 424 cm⁻¹ with a simultaneous broadening of the band from 45 to 71 cm⁻¹, which supports the assumption that defects in the nanoparticles increases, thus decreasing their sizes. A further increase in the temperature shifts the E_g peak to its initial value.

The Raman spectra of the modified samples after calcination at 300 and 500 $^{\circ}$ C show the peak at ca. 165 cm⁻¹, which can be attributed to a minor decrease in the lattice symmetry. This vibration disappears at elevated temperatures, which testifies to restoration of the structure.

As seen in Table 2, at similar calcination temperatures the half-widths of all peaks of the modified samples are greater than the half-widths of peaks of the samples without CeO_2 ; this testifies to a smaller size of the rutile particles with CeO_2 , which agrees with the XRD data.

3.3. BET

Investigation of the textural properties of rutile samples by low-temperature nitrogen adsorption revealed that in the entire range of temperatures the modified samples have a more developed pore structure with a higher specific surface area as compared to the zero sample (Table 3). All the samples with CeO₂ and pure rutile that were calcined at 300 and 500 °C have comparable pore volumes that range from 0.1 to 0.13 cm³/g. As the calcination temperature is raised, the pore volume values remain constant, whereas the specific surface area decreases and the average pore size increases; this testifies to implementation of the surface-diffusion sintering mechanism in the temperature range of 300 – 500 °C [15]. Pore broadening upon elevation of the calcination temperature from 300 to 500 °C is observed also on differential curves of the pore size distribution (Fig. 2). It should be noted that although the distribution curves are close to each other, the amount of thin pores with the effective diameter 3.5 nm

TABLE 3. Pore structure	parameters for nand	ostructured rutile	samples with	different CeO	D_2 content
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T_{calc} , °C	% CeO ₂	A_{BET} , m ² /g	$V_{\Sigma}, \ cm^3/g$	$\mathbf{D}_{pore},\mathbf{nm}$
300	0	48.9	0.11	8.7
	3	63.2	0.12	7.9
	5	76.9	0.13	6.6
	7	71.4	0.11	6.3
	10	62.2	0.10	6.8
500	0	35.3	0.11	13
	3	39.1	0.11	11.6
	5	42.4	0.11	10.4
	7	41.8	0.10	9.5
	10	39.2	0.10	10.2
700	0	5.1	0.03	27.7
	3	14.8	0.09	23.3
	5	15.1	0.08	22.6
	7	14.2	0.08	23.2
	10	14.5	0.08	21.8
1000	0	1.2	0.005	16.2
	3	2	0.006	11.7
	5	2.2	0.005	9.7
	7	2.1	0.006	11.9
	10	2.1	0.01	21

is greater in the modified samples than in pure rutile. Calcination at 700 and 1000 °C decreases both the specific surface area and the pore volume of all the samples; therewith, a decrease in the pore structure parameters for modified samples is less pronounced than for the calcined samples of pure rutile (Table 3). At 700 °C the specific surface area and pore volume of the samples with Ce are three times higher than the corresponding characteristics of pure rutile. The optimal ceria content in the samples is 5 wt.%. A further increase in the CeO₂ concentration does not produce an additional beneficial effect. At 1000 °C sintering of meso- and macropores occurs, the pore structure parameters are extremely low for all the samples, and these samples can be characterized as nonporous. The revealed regularities are clearly seen on differential curves of the pore size distribution for the series of 700 and 1000 °C samples (Fig. 2).



FIG. 2. Differential curves of the pore size distribution for the calcined rutile samples with different ceria content

3.4. HRTEM

High-resolution TEM images (Fig.3(a,b)) illustrate the intergrowth of pure rutile crystallites along interblock boundaries at 500 °C (Fig. 3(a)) and 700 °C (Fig. 3(b)). At 500 °C, the pore structure formed by narrow slit-like pores is retained (the pores are marked by arrows in the Figure 3). At 700 °C the pores virtually disappear. A different pattern is observed for the rutile sample modified with 5 % CeO₂ (Fig. 3(c,d)): the well developed pores between rutile crystallites are observed at both 500 °C (Fig. 3(c)) and 700 °C (Fig. 3(d)).

The TEM images also clearly demonstrate the difference in the crystallite sizes of rutile. The introduction of the Ce cation into the rutile matrix decreases the growth of its crystallites virtually by a factor of 2. Between rutile particles one can see the interlayers of weakly crystallized ceria (Fig. 3(d), within the oval), which prevent the intergrowth of rutile crystallites along the interblock boundaries. Fig. 3 displays TEM images only for the samples calcined at 500 and 700 $^{\circ}$ C, but this trend is observed also at other calcination temperatures.

It should be noted that the crystallized ceria phase was not detected in the samples calcined at 300 - 700 °C that were examined by XRD, Raman spectroscopy and TEM (using the measured interplanar distances). Most likely, titania inhibits the crystallization of ceria, which concentrates in the region of interblock boundaries of rutile



FIG. 3. High resolution TEM images of pure rutile samples calcined at 500 (a) and 700 $^{\circ}$ C (b) and rutile samples with the addition of 5 % CeO₂ calcined at 500 (c) and 700 $^{\circ}$ C (d)

in the amorphized state. And only upon calcination at 1000 $^{\circ}$ C a part of cerium is released as an oxide from the region of interblock boundaries with the formation of surface CeO₂ clusters and then the bulk CeO₂ phase having the fluorite structure.

4. Conclusion

TiO₂ (rutile) samples with the hierarchical 3D nanostructure were synthesized and modified with cerium cations; the effect of the modifying additive on the structural, textural and morphological properties of nanorutile was studied as a function of the calcination temperature. According to XRD, TEM, Raman spectroscopy and BET data, the introduction of 3 - 10 wt.% cerium into the rutile matrix decreases the growth of nanorutile crystallites at high temperatures ranging from 300 - 1000 °C and provides the formation of a more porous structure in comparison with unmodified samples. The optimal ceria content in the samples was found to be 5 wt.%. A further increase in the CeO₂ concentration does not produce an additional beneficial effect. Cerium cations are stabilized in the region of interblock boundaries or in the structural defects of TiO₂ and are released as the bulk CeO₂ phase only at 1000 °C, which does not exert a stabilizing effect at this temperature.

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