

## Annexure

Table 1 categorizes the 35 isomers of  $C_9H_{20}$  based on their branching. The corresponding chemical names (following IUPAC nomenclature) are given.

Table 1. Isomers of nonane

S.No	Number of carbons in spine	Isomers
1	9	$n$ -nonane ( $N_1$ ).
2	8	2-methyloctane( $N_2$ ), 3-methyloctane( $N_3$ ), 4-methyloctane( $N_4$ ).
3	7	(i) Dimethylheptanes 2,2-dimethylheptane( $N_5$ ), 2,3-dimethylheptane( $N_6$ ), 2,4-dimethylheptane( $N_7$ ), 2,5-dimethylheptane( $N_8$ ), 2,6-dimethylheptane( $N_9$ ), 3,3-dimethylheptane( $N_{10}$ ), 3,4-dimethylheptane( $N_{11}$ ), 3,5-dimethylheptane( $N_{12}$ ), 4,4-dimethylheptane( $N_{13}$ ). (ii) Ethylheptanes 3-ethylheptane( $N_{14}$ ), 4-ethylheptane( $N_{15}$ ).
4	6	(i) Trimethyl 2,2,3-trimethylhexane( $N_{16}$ ), 2,2,4-trimethylhexane( $N_{17}$ ), 2,2,5-trimethylhexane( $N_{18}$ ), 2,3,3-trimethylhexane( $N_{19}$ ), 2,3,4-trimethylhexane( $N_{20}$ ), 2,3,5-trimethylhexane( $N_{21}$ ), 2,4,4-trimethylhexane( $N_{22}$ ), 3,3,4-trimethylhexane( $N_{23}$ ). (ii) Methyl + Ethyl 3-ethyl-2-methylhexane( $N_{24}$ ), 4-ethyl-2-methylhexane( $N_{25}$ ), 3-ethyl-3-methylhexane( $N_{26}$ ), 3-ethyl-4-methylhexane( $N_{27}$ ).
5	5	(i) Tetramethyl 2,2,3,3-tetramethylpentane( $N_{28}$ ), 2,2,3,4-tetramethylpentane( $N_{29}$ ), 2,2,4,4-tetramethylpentane( $N_{30}$ ), 2,3,3,4-tetramethylpentane( $N_{31}$ ).

		(ii) Dimethyl + ethyl 3-Ethyl-2,2-dimethylpentane( $N_{32}$ ), 3-Ethyl-2,3-dimethylpentane( $N_{33}$ ), 3-Ethyl-2,4-dimethylpentane( $N_{34}$ ). (iii) Diethyl 3,3-diethylpentane( $N_{35}$ ).
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IUPAC nomenclature of isomers tabulated are verified in [15]

By using MATLAB, the spectrum, spectral radius, spectral gap, second largest eigenvalue, graph energy and eigenvalue-based graph entropy of all the isomers have been calculated and the results are tabulated in Table 2.

Table 2. Spectral parameters of nonane

Nonane isomers	Density	Spectrum	Spectral gap	Graph energy	Eigenvalue based Graph Entropy
$N_1$	0.7180	$\left\{ \pm 1.90211^{(1)}, \pm 1.61803^{(1)}, \right. \\ \left. \pm 1.17557^{(1)}, \pm 0.61803^{(1)}, 0^{(1)} \right\}$	0.23917	10.6275	0.8716
$N_2$	0.7140	$\left\{ \pm 1.96157^{(1)}, \pm 1.66294^{(1)}, \right. \\ \left. \pm 1.11114^{(1)}, \pm 0.39018^{(1)}, 0^{(1)} \right\}$	0.29863	10.2516	0.8484
$N_3$	0.7210	$\left\{ \pm 2^{(1)}, \pm 1.61803^{(1)}, \pm 1^{(1)}, \right. \\ \left. \pm 0.61803^{(1)}, 0^{(1)} \right\}$	0.38197	10.4721	0.8651
$N_4$	0.7200	$\left\{ \pm 2.01532^{(1)}, \pm 1.54801^{(1)}, \right. \\ \left. \pm 1.14288^{(1)}, \pm 0.48578^{(1)}, 0^{(1)} \right\}$	0.46731	10.3839	0.8582
$N_5$	0.7070	$\left\{ \pm 2.11688^{(1)}, \pm 1.63978^{(1)}, \right. \\ \left. \pm 0.91100^{(1)}, 0^{(1)} \right\}$	0.4771	9.3353	0.7549
$N_6$	0.7260	$\left\{ \pm 2.08397^{(1)}, \pm 1.57184^{(1)}, \right. \\ \left. \pm 1^{(1)}, \pm 0.43173^{(1)}, 0^{(1)} \right\}$	0.51213	10.1750	0.8472
$N_7$	0.7200	$\left\{ \pm 2.06082^{(1)}, \pm 1.59842^{(1)}, \right. \\ \left. \pm 1.09456^{(1)}, 0^{(1)} \right\}$	0.4624	9.5076	0.7644
$N_8$	0.7200	$\left\{ \pm 2.03565^{(1)}, \pm 1.69069^{(1)}, \right. \\ \left. \pm 0.88413^{(1)}, \pm 0.46476^{(1)}, 0^{(1)} \right\}$	0.34496	10.1504	0.8465
$N_9$	0.7060	$\left\{ \pm 2^{(1)}, \pm 1.73205^{(1)}, \pm 1^{(1)}, \right. \\ \left. 0^{(1)} \right\}$	0.2679	9.4641	0.7615
$N_{10}$	0.7200	$\left\{ \pm 2.16461^{(1)}, \pm 1.52804^{(1)}, \right. \\ \left. \pm 0.85362^{(1)}, \pm 0.50088^{(1)}, 0^{(1)} \right\}$	0.63657	10.0940	0.8459

$N_{11}$	0.7300	$\left\{ \begin{array}{l} \pm 2.11199^{(1)}, \pm 1.49637^{(1)}, \\ \pm 1^{(1)}, \pm 0.54806^{(1)}, 0^{(1)} \end{array} \right\}$	0.61562	10.3128	0.8574
$N_{12}$	0.7300	$\left\{ \begin{array}{l} \pm 2.07431^{(1)}, \pm 1.61803^{(1)}, \\ \pm 0.83500^{(1)}, \pm 0.61803^{(1)}, \\ 0^{(1)} \end{array} \right\}$	0.45628	10.2907	0.8568
$N_{13}$	0.7210	$\left\{ \begin{array}{l} \pm 2.17533^{(1)}, \pm 1.41421^{(1)}, \\ \pm 1.12603^{(1)}, 0^{(1)} \end{array} \right\}$	0.76112	9.4311	0.7614
$N_{14}$	0.7230	$\left\{ \begin{array}{l} \pm 2.04208^{(1)}, \pm 1.52023^{(1)}, \\ \pm 1^{(1)}, \pm 0.72028^{(1)}, 0^{(1)} \end{array} \right\}$	0.52185	10.5651	0.8711
$N_{15}$	0.7300	$\left\{ \begin{array}{l} \pm 2.05288^{(1)}, \pm 1.41421^{(1)}, \\ \pm 1.20864^{(1)}, \pm 0.56997^{(1)}, \\ 0^{(1)} \end{array} \right\}$	0.63867	10.4914	0.8656
$N_{16}$	0.7160	$\left\{ \begin{array}{l} \pm 2.21635^{(1)}, \pm 1.51211^{(1)}, \\ \pm 0.89516^{(1)}, 0^{(1)} \end{array} \right\}$	0.70424	9.2472	0.7509
$N_{17}$	0.7160	$\left\{ \begin{array}{l} \pm 2.16786^{(1)}, \pm 1.66159^{(1)}, \\ \pm 0.73450^{(1)}, 0^{(1)} \end{array} \right\}$	0.50627	9.1279	0.7420
$N_{18}$	0.7100	$\left\{ \begin{array}{l} \pm 2.13578^{(1)}, \pm 1.73205^{(1)}, \\ \pm 0.66215^{(1)}, 0^{(1)} \end{array} \right\}$	0.40373	9.0599	0.7367
$N_{19}$	0.7340	$\left\{ \begin{array}{l} \pm 2.23607^{(1)}, \pm 1.41421^{(1)}, \\ \pm 1^{(1)}, 0^{(1)} \end{array} \right\}$	0.82186	9.3005	0.7547
$N_{20}$	0.7350	$\left\{ \begin{array}{l} \pm 2.16461^{(1)}, \pm 1.52804^{(1)}, \\ \pm 0.85362^{(1)}, \pm 0.50088^{(1)}, \\ 0^{(1)} \end{array} \right\}$	0.63657	10.0943	0.8459
$N_{21}$	0.7180	$\left\{ \begin{array}{l} \pm 2.11688^{(1)}, \pm 1.63978^{(1)}, \\ \pm 0.91100^{(1)}, 0^{(1)} \end{array} \right\}$	0.4771	9.3353	0.7549
$N_{22}$	0.7200	$\left\{ \begin{array}{l} \pm 2.19399^{(1)}, \pm 1.59038^{(1)}, \\ \pm 0.81060^{(1)}, 0^{(1)} \end{array} \right\}$	0.60361	9.1899	0.7467
$N_{23}$	0.7410	$\left\{ \begin{array}{l} \pm 2.24698^{(1)}, \pm 1.41421^{(1)}, \\ \pm 0.80194^{(1)}, \pm 0.55496^{(1)}, \\ 0^{(1)} \end{array} \right\}$	0.83277	10.0361	0.8453
$N_{24}$	0.7290	$\left\{ \begin{array}{l} \pm 2.11917^{(1)}, \pm 1.41421^{(1)}, \\ \pm 1.15904^{(1)}, \pm 0.40713^{(1)}, \\ 0^{(1)} \end{array} \right\}$	0.70496	10.1991	0.8479
$N_{25}$	0.7190	$\left\{ \begin{array}{l} \pm 2.08397^{(1)}, \pm 1.57184^{(1)}, \\ \pm 1^{(1)}, \pm 0.43173^{(1)}, \\ 0^{(1)} \end{array} \right\}$	0.51213	10.1750	0.8472
$N_{26}$	0.7370	$\left\{ \begin{array}{l} \pm 2.20595^{(1)}, \pm 1.33763^{(1)}, \\ \pm 1^{(1)}, \pm 0.58699^{(1)}, \\ 0^{(1)} \end{array} \right\}$	0.86832	10.2611	0.8570
$N_{27}$	0.7360	$\left\{ \begin{array}{l} \pm 2.13578^{(1)}, \pm 1.41421^{(1)}, \\ \pm 1^{(1)}, \pm 0.66215^{(1)}, \\ 0^{(1)} \end{array} \right\}$	0.72157	10.4242	0.8649
$N_{28}$	0.7530	$\left\{ \begin{array}{l} \pm 2.33441^{(1)}, \pm 1.41421^{(1)}, \\ \pm 0.74196^{(1)}, 0^{(1)} \end{array} \right\}$	0.9202	8.9811	0.7360
$N_{29}$	0.7350	$\left\{ \begin{array}{l} \pm 2.25525^{(1)}, \pm 1.55821^{(1)}, \\ \pm 0.69704^{(1)}, 0^{(1)} \end{array} \right\}$	0.69704	9.0209	0.7367

$N_{30}$	0.7200	$\left\{ \begin{array}{l} \pm 2.23607^{(1)}, \pm 1.73205^{(1)}, \\ 0^{(1)} \end{array} \right\}$	0.50402	7.9362	0.5985
$N_{31}$	0.7350	$\left\{ \begin{array}{l} \pm 2.28825^{(1)}, \pm 1.41421^{(1)}, \\ 0.87403^{(1)}, 0^{(1)} \end{array} \right\}$	0.87404	9.1529	0.7465
$N_{32}$	0.7310	$\left\{ \begin{array}{l} \pm 2.23607^{(1)}, \pm 1.41421^{(1)}, \\ \pm 1^{(1)}, 0^{(1)} \end{array} \right\}$	0.82186	9.3005	0.7547
$N_{33}$	0.7510	$\left\{ \begin{array}{l} \pm 2.26382^{(1)}, \pm 1.27932^{(1)}, \\ \pm 1^{(1)}, \pm 0.48831^{(1)}, \\ 0^{(1)} \end{array} \right\}$	0.9845	10.0629	0.8461
$N_{34}$	0.7340	$\left\{ \begin{array}{l} \pm 2.17533^{(1)}, \pm 1.41421^{(1)}, \\ \pm 1.12603^{(1)}, 0^{(1)} \end{array} \right\}$	0.76112	9.43115	0.7614
$N_{35}$	0.7500	$\left\{ \begin{array}{l} \pm 2.23607^{(1)}, \pm 1^{(1)}, \pm 1^{(1)}, \\ \pm 1^{(1)}, 0^{(1)} \end{array} \right\}$	1.23607	10.4721	0.8708

Density of nonane in column 2 are taken from [20]